

Istanbul, 7-11 July





Beyond Access: Analyzing the National Multimodal Public Transportation Network with Big Data and Functional Urban Area

Author's Name: Baekchan Jeon*, Myounggu Kang**

Affilation: Department of Urban Planning & Design, University of Seoul, Republic of Korea

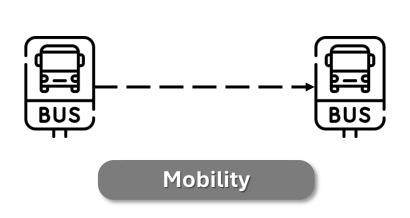
Graduate student (Master's program)

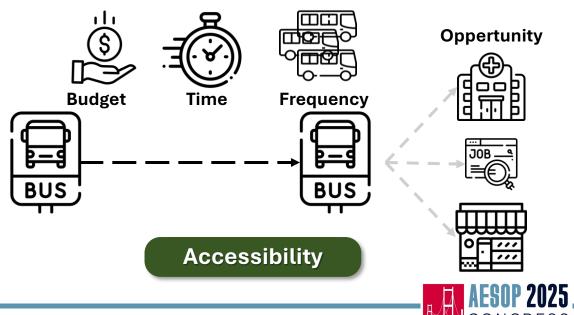
Emal: sarakael0602@uos.ac.kr*, mk@uos.ac.kr**



Introduction

- •The goal of public transport is not just **Mobility**, but ensuring equitable **Accessibility** to opportunities (Geurs & Van Wee, 2004).
- •True accessibility is a multidimensional concept defined by **Quality of Service**, including frequency, travel time, and transfer convenience (Bertolini et al., 2005; Kujala et al., 2018).
- •This is a matter of **transport justice**, ensuring social inclusion for all citizens (Lucas, 2012; Verlinghieri & Schwanen, 2020).





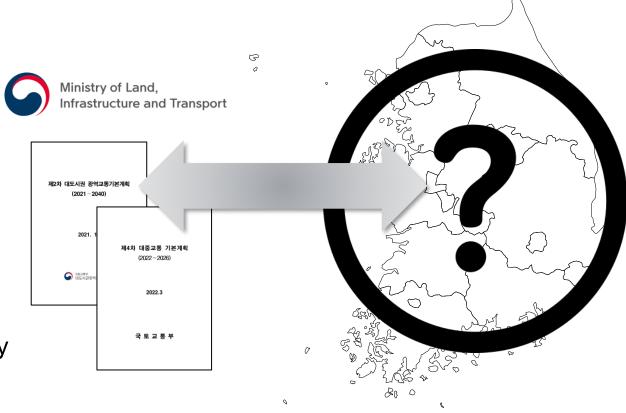
The Policy Imperative & The Research Gap

The Vision

The Korean government aims for a "hyper-connected" nation with reduced travel times and inclusive services (MOLIT, 2021a; 2022).

The Gap

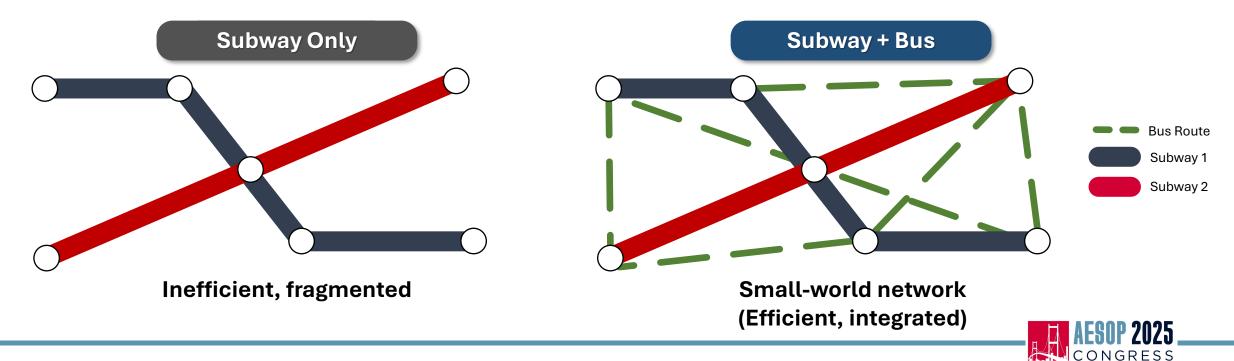
Are these national goals being met? A comprehensive, evidence-based evaluation framework for the *entire national system* from the perspective of *actual living areas* is critically lacking.





The First Flaw: The Single-Mode Illusion

- •Urban transport is an interdependent multilayer network (Aleta et al., 2017; Kurant & Thiran, 2006).
- •Analyzing modes in isolation provides a **dangerously distorted picture** of system performance and resilience (Gattuso & Miriello, 2005).
- •The synergy between modes can fundamentally alter our evaluation of the system's efficiency.

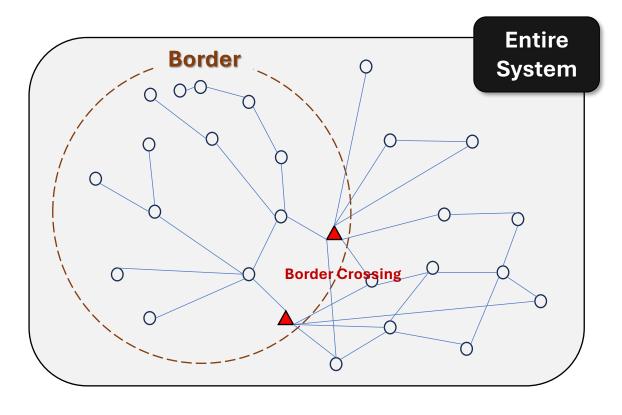


The Second Flaw: The "Edge Effect" of Artificial Boundaries

- •Network centrality is a **global property**, determined by the entire network's topology (Freeman, 1978).
- Analyzing a network within artificial boundaries
 (e.g., city limits) systematically underestimates
 the importance of edge nodes

(Porta et al., 2006a; Buhl et al., 2006).

•This leads to flawed resource allocation and policy decisions.



A critical hub becomes a mere periphery

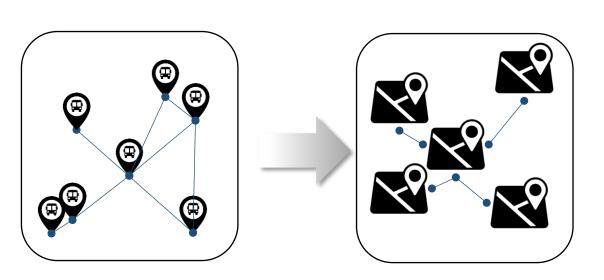


A Two-Fold Paradigm Shift is Needed

•To overcome these flaws, we must fundamentally shift our analytical paradigm in two dimensions.

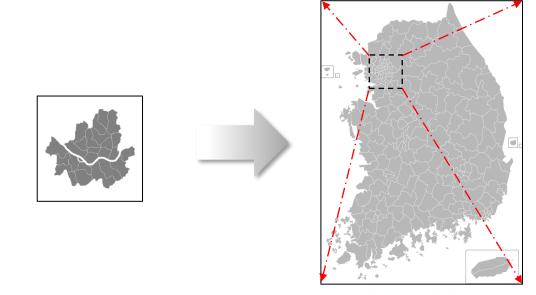
Shift in Unit

From Points (Stops) → To Areas (Living Spheres)



Shift in Scope

From a City (Fragmented) → To the Nation (Holistic)





Shift 1: From Points to Functional Areas

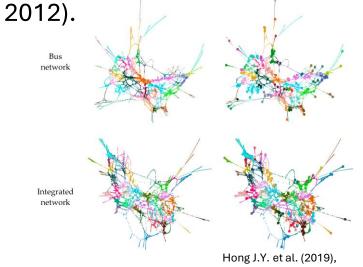
Previous

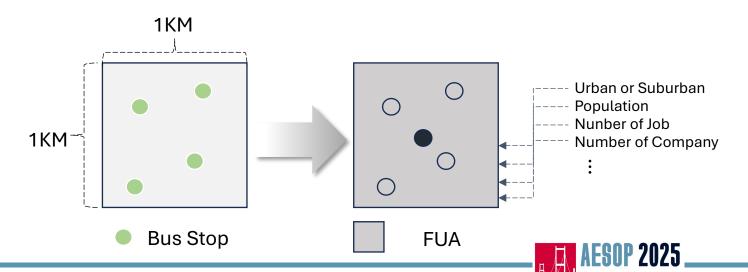
Point-to-Point models based on stops are insufficient for macro-policy insights.

My Approach

Area-to-Area models using **Functional Urban Areas** (**FUAs**).

(FUAs). This aligns the analysis with how human mobility is actually structured within hierarchical "spatial containers" (Alessandretti et al., 2020) and reflects policy-makers' interests in functional regions (OECD,

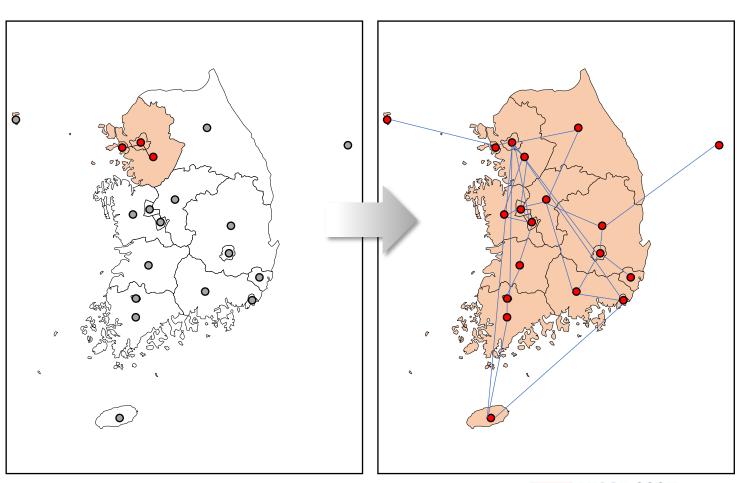




OECD et al. (2021), Applying the Degree of Urbanisation

Shift 2: From Bounded Cities to the Holistic Nation

- •The only way to eliminate the **"edge effect"** is to expand the scope to a **closed system** (Strahler, 1952; Porta et al., 2006b).
- •For domestic transport, the **entire nation** is the most logical closed system.
- •This approach ensures technical accuracy and enables a comprehensive evaluation of interregional connectivity and equity.





The Enabler: Big Data & Advanced Computing

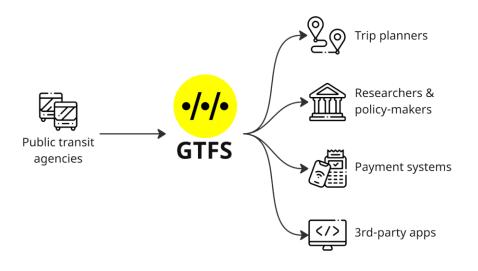
This approach has only recently become possible.

The Breakthrough

Standardized national **GTFS(General Transit Feed Specification) Big Data** (Kujala et al., 2018; Zhong et al., 2016).

High-Performance Computing

Using Distributed processing (Dask) and GPU acceleration (NVIDIA RAPIDS) to handle massive scale (~200k nodes, ~33M edges).







Accelerated with





Research Framework: Methodology Overview

This slide visually summarizes the entire research flow from raw data to policy insights.

Step 0 – Data Processing

Nationwide GTFS Data (Bus, Express Bus, Subway, Railway, Aviation, Maritime)

Step 1 - Point-to-Point Network

Build raw edge list (33M+ edges). Data cleaning based on speed profiles.

Step 2 - Multilayer Model

Network

Construct 6 "Super Layers" (one for each mode) using a complete-graph approach within each route.

Step 3 - Weighted Network

Analysis

Aggregate the network to FUA polygons. Analysis network topology metrics (Centrality, etc.) using frequency as weights to measure the actual service level.

Step 4 - Synthesis & Policy

Insights

Correlate the calculated service level metrics with socio-economic data.



Building the Network: A Two-Step Aggregation Framework

Level 1: Route Layer

Raw GTFS data. Each of the 25,000 bus routes is a separate layer. Contains massive redundancy and overlap.

Level 2: Super Layer

A Point-to-Point network for each transportation mode.
Reveals the infrastructural connectivity of the entire mode.

Level 3: FUA Layer

An Area-to-Area network.
Reveals the macro-level
functional connectivity between
living spheres.

Consolidate all routes of the same mode.

Parallel edges between the same two stops are

merged into a single, weighted edge

Aggregate all stops within the same Functional Urban Area into a single node.

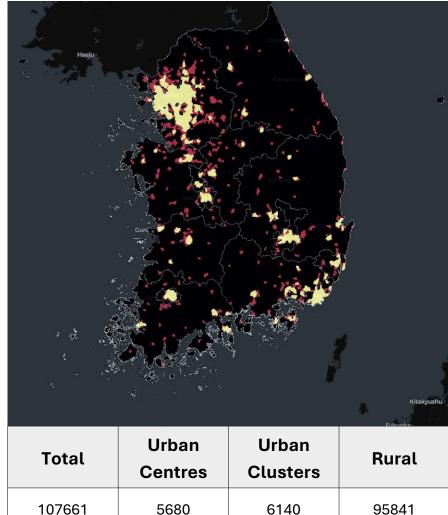


Used Dataset

| Data | Contents | Year | Source |
|--|---|-------------|--------|
| GTFS (General Transit Feed Specification) | Nationwide GTFS Data for Bus, Express Bus, Subway, Railway, Aviation, Maritime | 2024. 12 | TMAP |
| Urbanization Area GRID | The 1 km x 1 km grid SHP file based on the FUA methodology includes data on population, households, businesses, and number of employees, as well as Urban centres, Urban clusters, and Rural classifications. | 2022 | SGIS |

Transportation

| Mode | Number of Stops | Number of Routes | Number of Edges | Operation Frequency |
|-------------|--------------------|------------------|--------------------|------------------------|
| Subway | 1,082 | 57 | 50,144 | 5,398,849 |
| Bus | 192,411 | 24,973 | 33,957,996 | 791,064,563 |
| Express Bus | 1,426 | 11,851 | 18,332 | 87,540 |
| Railway | 235 | 12,807 | 12,807 | 56,911 |
| Aviation | 13 | 34 | 34 | 468 |
| Maritime | 340 | 2,335 | 2,335 | 4,632 |
| Total | 195,507 | 52,057 | 34,041,648 | 796,612,963 |



| Total | Urban Centres | Urban Clusters | Rural |
|--------|------------------|-------------------|-------|
| 107661 | 5680 | 6140 | 95841 |



Research Questions & Key Contributions

RQ1 What is the true structure of Korea's national public transport network when viewed holistically?

RQ2 How does the actual level of service (beyond mere access) vary across different regions and transport modes?

What is the relationship between this quantified service level and key socio-economic characteristics?

A New Lens (FUA Nodes)

RQ3

Overcomes the 'edge effect' and provides macro-level insights relevant for policy (Porta et al., 2006a; OECD, 2012).

A Complete Picture (Multilayer Network)

Avoids the single-mode illusion by integrating all transport modes (Aleta et al., 2017; Latora & Marchiori, 2002).

Beyond "Access" (Weighted Analysis):

Evaluates actual service quality by incorporating frequency, not just connectivity (Bertolini et al., 2005).



What Aggregation Reveals: The Functional Hierarchy of Transport

| Mode | Number of Stops | Number of Routes | Number of Link | Number of Link | Number of Link | Route → Super Layer (Preservation Rate 1) | Super → FUA Layer (Preservation Rate 2) |
|-------------|--------------------|------------------|-------------------|-------------------|-------------------|---|---|
| | Ciopo | 1104100 | Route Layer | Super Layer | FUA Layer | 82% | 86% |
| Subway | 1,082 | 57 | 50,144 | 41,262 | 35,471 | 52% | 12% |
| Bus | 192,411 | 24,973 | 33,957,996 | 17,825,689 | 2,119,588 | 88% | 81% |
| Express Bus | 1,426 | 11,851 | 18,332 | 16,196 | 13,072 | 72% | 100% |
| Railway | 235 | 12,807 | 12,807 | 9,252 | 9,248 | 100% | 100% |
| Aviation | 13 | 34 | 34 | 34 | 34 | 100% | 87% |
| Maritime | 340 | 2,335 | 2,335 | 2,335 | 2,041 | | |

Step 1: Consolidating Service Redundancy Step 2: Identifying Functional Scale & Role

Bus: 48% of links are redundant routes.

Bus (12%): → High Consolidation reveals Local / Capillary role.

Massive link reduction due to:

Numerous Intra-FUA links.

Redundant Inter-FUA links between various stops.

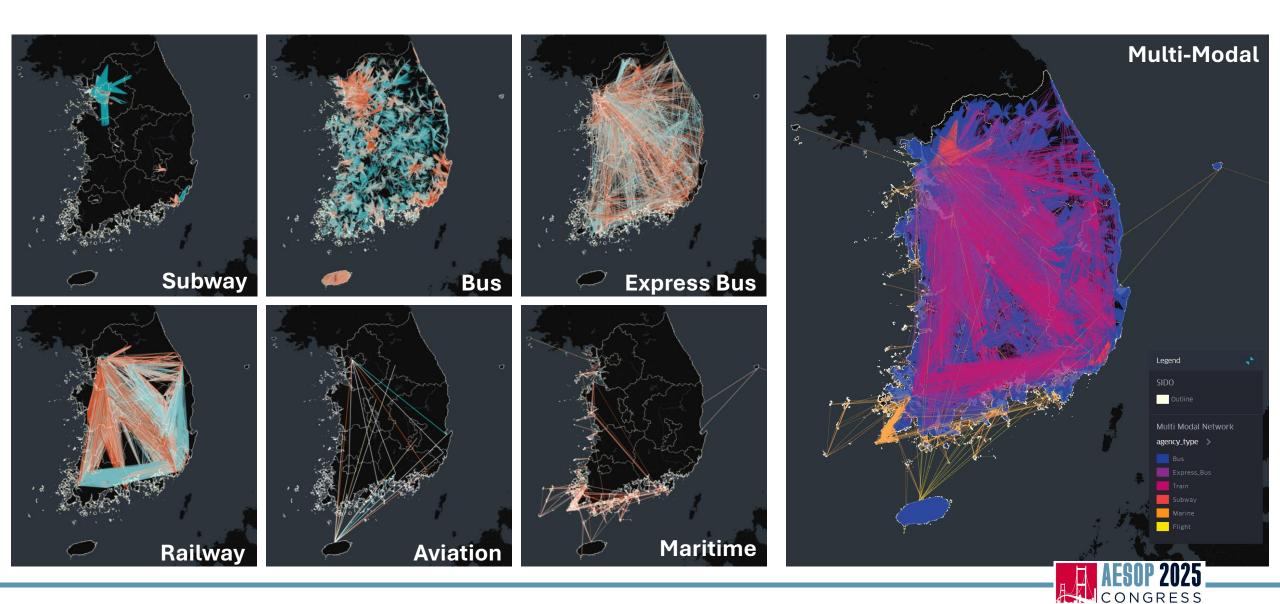
Railway (100%): → No Consolidation reveals National / Trunk role.

Each stop-to-stop link represents a unique area-to-area connection.

Methodology reveals the Functional Hierarchy of the national transport system.



Multimodal Public Transport Network Visualization



Macro-Structure: Connectivity and Fragmentation

| Туре | Num Vertices | Num Edges | Density | Global Clustering Coefficient | LCC Ratio |
|-----------------------|--------------|-----------|---------|-------------------------------|-----------|
| Subway | 827 | 35471 | 0.052 | 0.691 | 0.69 |
| Bus | 41283 | 2119588 | 0.001 | 0.445 | 0.98 |
| Express_Bus | 1040 | 13072 | 0.012 | 0.306 | 1.00 |
| Railway | 234 | 9248 | 0.170 | 0.642 | 1.00 |
| Aviation | 12 | 34 | 0.258 | 0.199 | 1.00 |
| Maritime | 293 | 2041 | 0.024 | 0.762 | 0.78 |
| Multiplex (All Modes) | 41552 | 2179454 | 0.001 | 0.430 | 1.00 |

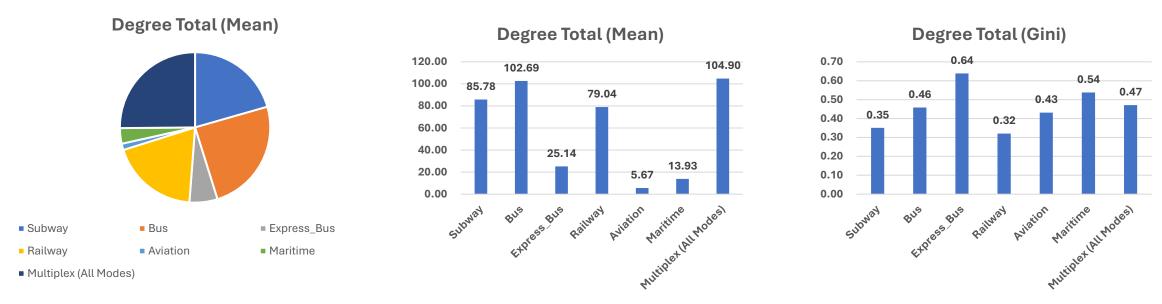
- •High Clustering (Subway, Maritime): Networks are formed by tightly-knit regional clusters.
- •Regional Fragmentation (Subway, Maritime): LCC Ratio < 1.0 indicates that these modes operate in geographically disconnected pockets (e.g., Seoul vs. Busan subway).
- •National Integration: The Multiplex (All Modes) network forms a single, fully connected system (LCC Ratio = 1.00).



Connectivity Structure: Ubiquitous vs. Hierarchical

| Туре | Degree Total (Mean) | Degree Total (Std) | Degree Total (CV) | Degree Total (Gini) |
|--------------------------|---------------------|--------------------|-------------------|---------------------|
| Subway | 85.78 | 58.72 | 0.68 | 0.35 |
| Bus | 102.69 | 106.76 | 1.04 | 0.46 |
| Express_Bus | 25.14 | 40.79 | 1.62 | 0.64 |
| Railway | 79.04 | 45.76 | 0.58 | 0.32 |
| Aviation | 5.67 | 5.82 | 1.03 | 0.43 |
| Maritime | 13.93 | 17.05 | 1.22 | 0.54 |
| Multiplex (All Modes) | 104.90 | 115.78 | 1.10 | 0.47 |

Connectivity Structure: Ubiquitous vs. Hierarchical



- •Ubiquitous Connector (Bus): The highest mean degree signifies that the bus network connects to the most diverse range of areas.
- •Hierarchical Hub-and-Spoke (Express Bus): The highest Gini coefficient indicates a strong hierarchical structure. A few hub terminals connect to many destinations, while most others have few connections.
- •Egalitarian Structure (Railway): The lowest Gini coefficient suggests a more balanced and linear connection structure.

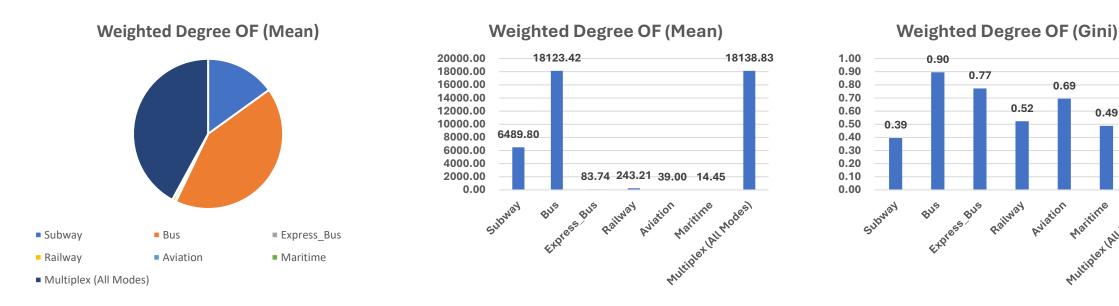


Service Level Analysis: The Overwhelming Dominance of Local Transit

| Туре | Weighted Degree OF (Mean) | Weighted Degree OF (Std) | Weighted Degree OF (CV) | Weighted Degree OF (Gini) |
|-----------------------|---------------------------|--------------------------|-------------------------|---------------------------|
| Subway | 6489.80 | 5280.23 | 0.81 | 0.39 |
| Bus | 18123.42 | 65246.84 | 3.60 | 0.90 |
| Express_Bus | 83.74 | 215.88 | 2.58 | 0.77 |
| Railway | 243.21 | 286.18 | 1.18 | 0.52 |
| Aviation | 39.00 | 61.37 | 1.57 | 0.69 |
| Maritime | 14.45 | 14.64 | 1.01 | 0.49 |
| Multiplex (All Modes) | 18138.83 | 65702.98 | 3.62 | 0.90 |



Service Level Analysis: The Overwhelming Dominance of Local Transit



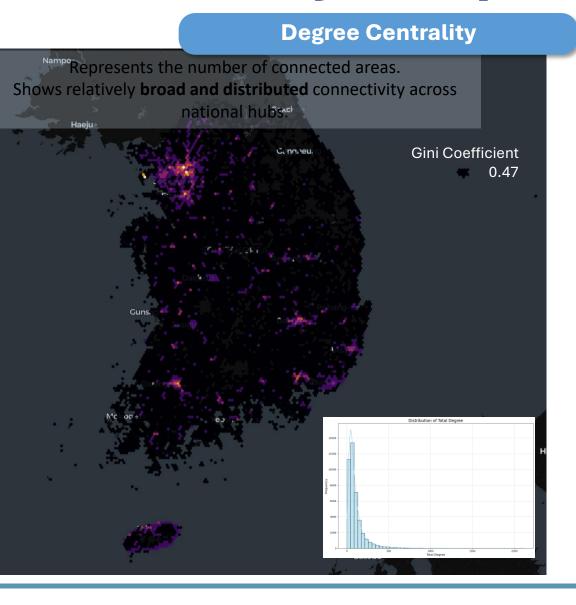
•Dominance in Service Volume: Bus and Subway overwhelmingly dominate the total volume of public transport services.

0.90

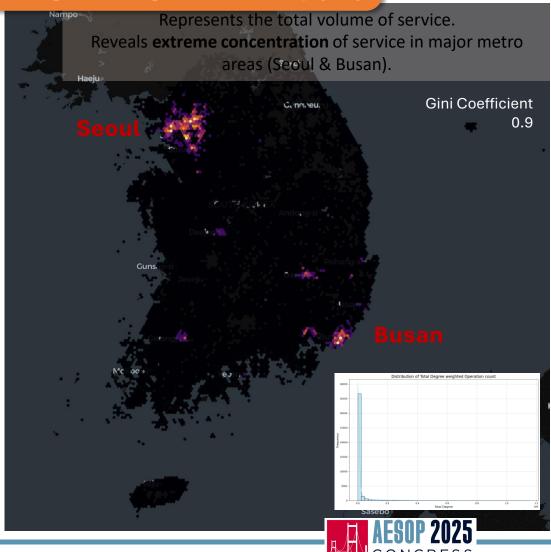
0.49

- •Extreme Inequality (Bus): The Gini coefficient of 0.90 for the bus network reveals a "hyper-hierarchical" structure in service levels.
- •The Punchline: While the bus network connects everywhere (ubiquity), the actual high-frequency services are extremely concentrated on a few key corridors.

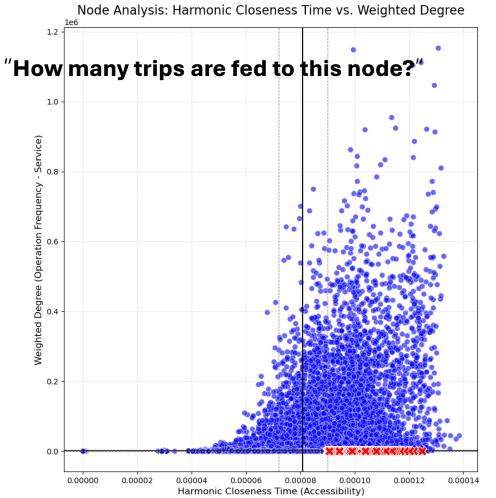
Connectivity and Operation Frequency

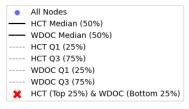


Weighted Degree Centrality (OF)



A 2D Framework for Node Classification: Accessibility vs. Service Level





| HCT_Categ | WDOC_Category | | | |
|--------------------------|---------------------------|---------------------|---------------------|--|
| ory | L_WDOC (Bottom 25%) | M_WDOC (25%-75%) | H_WDOC (Top 25%) | |
| L_HCT (Bottom 25%) | 2914 | 5791 | 1683 | |
| M_HCT (25%-75%) | 5642 | 10610 | 4524 | |
| H_HCT (Top 25%) | 1850 | 4359 | 4179 | |

Harmonic Closeness Centrality

$$H_i = \sum_{j \neq i} \frac{1}{d(i,j)}$$

d(i,j): Shortest path time based distance from i to j

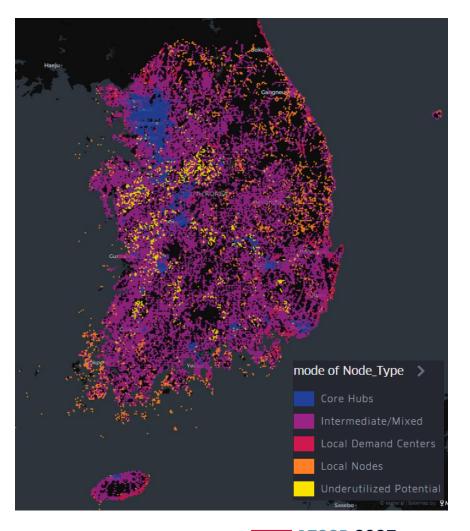
- •All nodes are plotted based on these two key metrics.
- •The plot is divided into quadrants by the median/quartiles to classify each node into a specific archetype.



[&]quot;How easy is it for this node to reach the rest of the network?"

Four Faces of the Network: A National Node Typology

| | Low Service Volume | High Service Volume |
|-----------------------|--|--|
| High Accessibility | Underutilized Potential High accessibility, low service need to expand/streamline services 4.45% (1,850) | Core Hubs High Access, High Service The Heart of the National Network 10.06% (4,179) |
| Low Accessibility | Local Nodes Low accessibility, low service local transit-oriented 7.01% (2,914) | Local Demand Centers Low access, high service high demand exists in the region 4.05% (1,683) |





Conclusion: Summary of Key Findings

A Functionally Differentiated Ecosystem

The national transport network operates as a complementary ecosystem of **Trunk Networks** (Rail, Express Bus) and **Capillary Networks** (Bus, Subway).

The Gap Between Connectivity & Service

A significant gap exists between potential connectivity (reach) and actual service levels (volume). Service volume is **extremely concentrated** in major metropolitan areas (Seoul & Busan).

A New Typology for Policy

Functional areas (nodes) can be classified into four distinct archetypes: Core Hubs, Underutilized Potential, Local Demand Centers, and Local Nodes.



Discussion & Policy Implications

Beyond Infrastructure Expansion → Towards System Optimization

Shift policy focus from simply building new lines to optimizing the existing multi-layered system.

Data-Driven, Targeted Investment

Utilize the node typology for targeted strategies: enhance 'Core Hubs', activate 'Underutilized Potential', and improve connectivity for 'Local Demand Centers'.

A New Tool for Evaluation & Monitoring

Our framework provides a more realistic tool for evaluating the effectiveness of national and regional transport plans.



Limitations & Future Research

Limitations

- **Static Analysis:** This study uses a static GTFS snapshot, not capturing real-time dynamics or demand fluctuations.
- **Supply-Side Focus:** The analysis is based on service supply, not yet incorporating actual passenger demand data (e.g., smart cards).
- Simplified Weights: Weights are based on frequency; incorporating time, cost, and transfer penalties would offer a more nuanced view.

Future Research

- Temporal Network Analysis: Analyzing network changes over time (daily, weekly, seasonal).
- Integrating Demand Data: Combining supply (GTFS) with demand (smart card data) to model actual passenger flows.
- Policy Simulation: Using the model to simulate the network-wide impact of new projects or policy changes (e.g., "What if we add a new Subway line?").



Thank you!



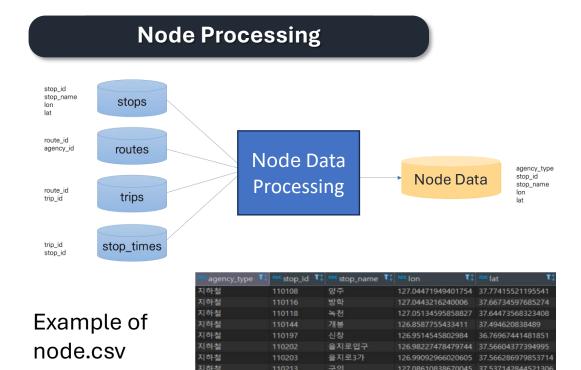
Appendix: The contents of a GTFS feed

| Filename | Required | Defines |
|---------------------|----------|---|
| agency.txt | Required | One or more transit agencies that provide the data in this feed. |
| calendar.txt | Required | Dates for service IDs using a weekly schedule. Specify when service starts and ends, as well as days of the week where service is available. |
| calendar_dates.txt | Optional | Exceptions for the service IDs defined in the calendar.txt file. If calendar_dates.txt includes ALL dates of service, this file may be specified instead of calendar.txt. |
| fare_attributes.txt | Optional | Fare information for a transit organization's routes. |
| fare_rules.txt | Optional | Rules for applying fare information for a transit organization's routes. |
| feed_info.txt | Optional | Additional information about the feed itself, including publisher, version, and expiration information. |
| frequencies.txt | Optional | Headway (time between trips) for routes with variable frequency of service. |
| routes.txt | Required | Transit routes. A route is a group of trips that are displayed to riders as a single service. |
| shapes.txt | Optional | Rules for drawing lines on a map to represent a transit organization's routes. |
| stop_times.txt | Required | Times that a vehicle arrives at and departs from individual stops for each trip. |
| stops.txt | Required | Individual locations where vehicles pick up or drop off passengers. |
| transfers.txt | Optional | Rules for making connections at transfer points between routes. |
| trips.txt | Required | Trips for each route. A trip is a sequence of two or more stops that occurs at specific time. |

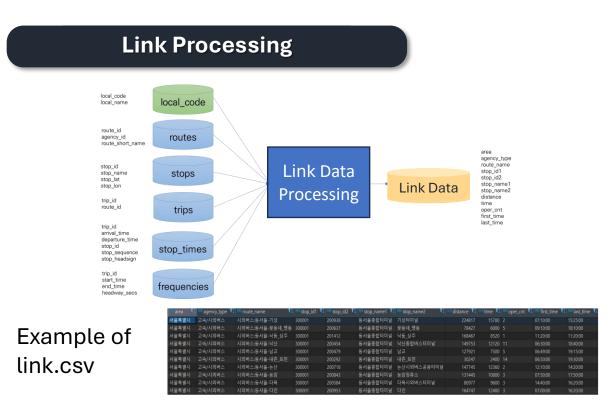
The contents of a GTFS feed. Despite the .txt filename extensions, all files are comma-separatedvalues (CSV) files. This table is an excerpt from the "General Transit Feed Specification Reference" (https://developers.google.com/transit/gtfs/reference/) by Google LLC, licensed under http://creativecommons.org/licenses/by/3.0/CC BY 3.0.



Appendix: Data Processing Based on GTFS Format



Using the stops, routes, trips, and stop_times information from the GTFS dataset, we extracted basic attributes such as the ID, name, and location of each stop to build detailed information about the stops.



Using the routes, stops, trips, stop_times, and frequencies information from the GTFS dataset, we derived combinations of departure and arrival stops that can be traveled between without transfers for each route.



Appendix: Network Construction Framework

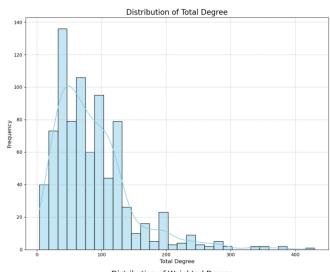
| Process Stage | Intuitive Definition | Formulation |
|---------------|---|--|
| Route Layer | Considering an individual route (r) as a layer. Direct connection of all pairs of stops (i, j) belonging to the same route. | $G_r = (V, E_r)$ where an edge (i,j) in E_r exists if stop i,j |
| Super Layer | Consolidate all routes within a mode of transportation m. The frequency of all overlapping routes connecting the same two stops (i,j) is summed to create a single weighted trunk line for transportation m. | $A \ Point - to - Point \ graph \ G_S^m$ $= (V, E_S^m, W_S^m).$ $he \ weight \ of \ an \ edge \ (i,j) for \ mode \ m \ is:$ $w_{ij}^{\{S,m\}} = \sum_{\{r \in R_m\}} f_{\{ijr\}}$ • R_m : The set of all routes d belonging to transportation mode m |
| FUA Layer | Aggregate the stops of mode m into functional areas (FUAs). Sum the weights of all "stop-to-stop" connections of mode m between two FUAs (f_a, f_b) to create a "region-to-region" connection for mode m. | $An \ Area - to - Area \ graph \ G_F^m$ $= (F, E_F^m, W_F^m).$ $The \ weight \ of \ an \ edge \ (f_a, f_b) for \ mode \ m \ is:$ $w_{\{ab\}}^{\{F,m\}} = \sum_{\{i \in f_a, j \in f_b\}} w_{\{ij\}}^{\{S,m\}}$ $AESOP \ 2025$ |
| | | CONGRESS |

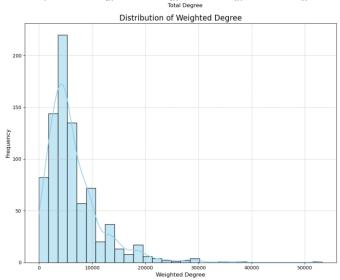
Appendix: Network Analysis Metrics

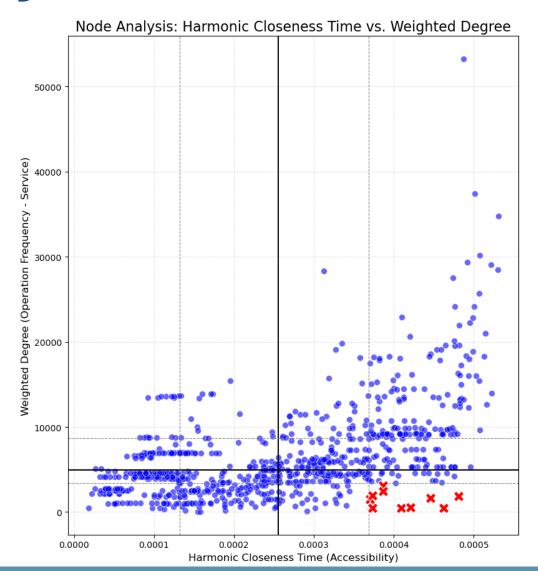
| Metric | Intuitive Definition | Mathematical Fo | rmula |
|----------------------------------|--|--|--|
| Degree Centrality | How many other nodes a node (region) is directly connected to (extent of connectivity). | $k_i = \sum_{j=1}^{N} A_{ij}$ | A_{ij} : i if connected j , =1 , \neq 0 |
| Weighted Degree Centrality | The sum (weighted) number of trips of all connections to a node. (actual service delivery) | $s_i = \sum_{j=1}^N w_{ij}$ | w_{ij} : i if connected j , Operation Frequency weighting of connections |
| Density | How many actual connections exist out of all possible connections (network denseness). | Number of Edges Maximum Possible Edges | |
| Global Clustering Coefficient | How strong is the tendency for "my friend's friend is my friend" across the network (degree of network cohesion). | $C = \frac{3 \times (number\ of\ triangles)}{(number\ of\ connected\ triplets)}$ | |
| LCC Ratio | Percentage of nodes that belong to the largest connectivity network, out of all nodes. (Integrity/disjointness of the network) | Nodes in Largest Connected Component Total Number of Nodes | |
| Coefficient of Variation (CV) | Standard deviation relative to the mean. Indicates the relative variability of the distribution. (relative unevenness of connectivity) | $CV = \frac{\sigma_k}{\mu_k}$ | μ_k : Mean σ_{k_k} : Standard deviation |
| Gini Coefficient | Used to measure income inequality. 0 (perfect equality) to 1 (perfect inequality). (absolute inequality in connectivity) | $G = \frac{\sum_{i=1}^{n} \sum_{j=1}^{n} x_i - x_j }{2\sum_{i=1}^{n} \sum_{j=1}^{n} x_j}$ | |
| Harmonic Closeness Centrality | How easy it is for one node to reach all other nodes (accessibility of the network). | $H_i = \sum_{j \neq i} \frac{1}{d(i,j)}$ | d(i,j): Shortest path time based distance from i to j |



Appendix: Subway Network





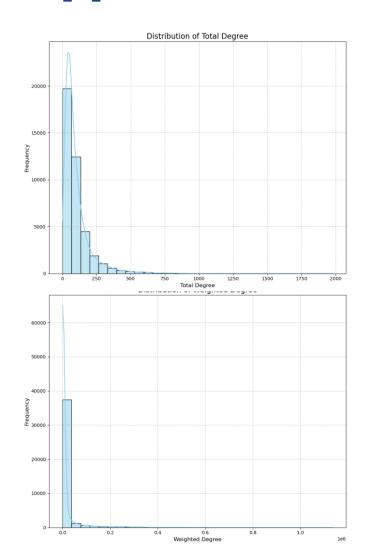


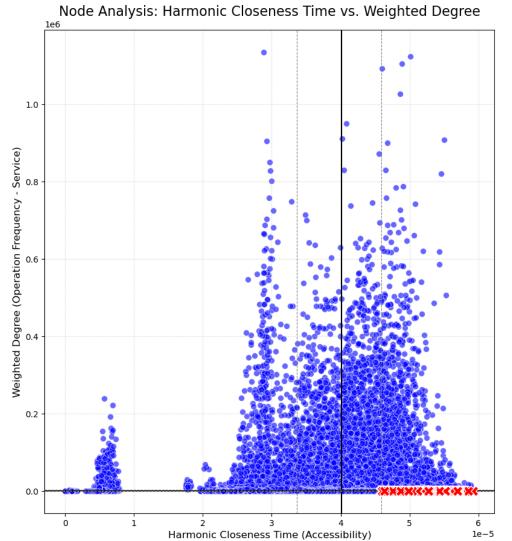
| • | All Nodes |
|---|-----------------------------------|
| _ | HCT Median (50%) |
| _ | WDOC Median (50%) |
| | HCT Q1 (25%) |
| | HCT Q3 (75%) |
| | WDOC Q1 (25%) |
| | WDOC Q3 (75%) |
| × | HCT (Top 25%) & WDOC (Bottom 25%) |

| HCT_Cate gory | WDOC_Category | | |
|--------------------------|---------------------------|-------------------------|---------------------|
| | L_WDOC (Bottom 25%) | M_WDOC (25%- 75%) | H_WDOC (Top 25%) |
| L_HCT (Bottom 25%) | 76 | 115 | 16 |
| M_HCT (25%- 75%) | 121 | 239 | 53 |
| H_HCT (Top 25%) | 10 | 59 | 138 |



Appendix: Bus Network



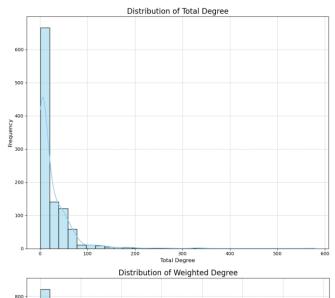


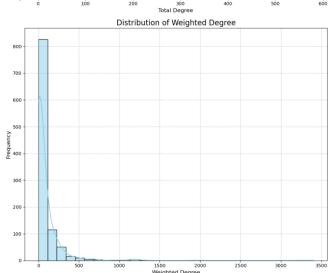
| • | All Nodes |
|---|-----------------------------------|
| _ | HCT Median (50%) |
| _ | WDOC Median (50%) |
| | HCT Q1 (25%) |
| | HCT Q3 (75%) |
| | WDOC Q1 (25%) |
| | WDOC Q3 (75%) |
| × | HCT (Top 25%) & WDOC (Bottom 25%) |

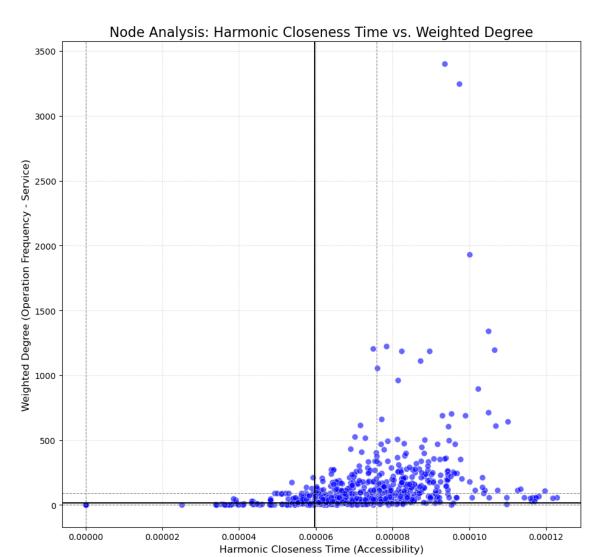
| HCT_Cate gory | WDOC_Category | | |
|--------------------------|---------------------------|-------------------------|---------------------|
| | L_WDOC (Bottom 25%) | M_WDOC (25%- 75%) | H_WDOC (Top 25%) |
| L_HCT (Bottom 25%) | 2261 | 5154 | 2906 |
| M_HCT (25%- 75%) | 5356 | 10187 | 5098 |
| H_HCT (Top 25%) | 2714 | 5290 | 2317 |



Appendix: Express Bus Network





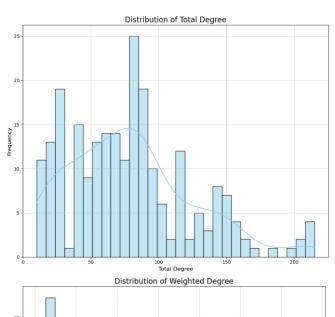


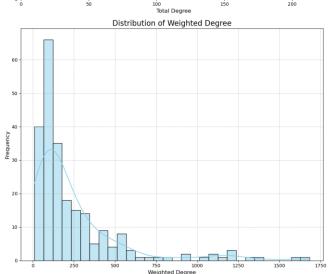
| • | All Nodes |
|---|-------------------|
| _ | HCT Median (50%) |
| _ | WDOC Median (50%) |
| | HCT Q1 (25%) |
| | HCT Q3 (75%) |
| | WDOC Q1 (25%) |
| | WDOC Q3 (75%) |

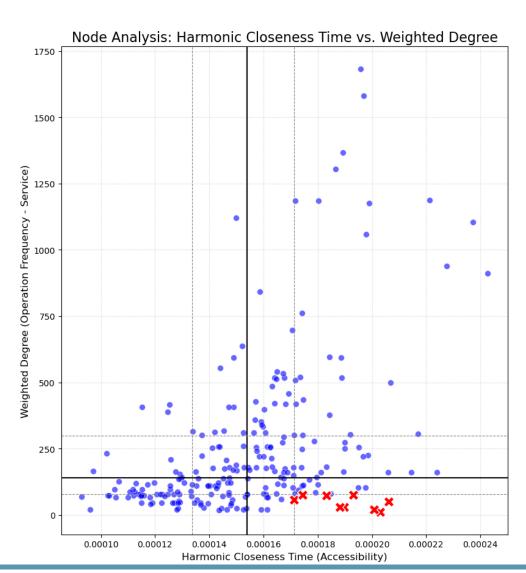
| HCT_Cate gory | WDOC_Category | | |
|--------------------------|---------------------------|-------------------------|---------------------|
| | L_WDOC (Bottom 25%) | M_WDOC (25%- 75%) | H_WDOC (Top 25%) |
| L_HCT (Bottom 25%) | 398 | 0 | 0 |
| M_HCT (25%- 75%) | 0 | 292 | 90 |
| H_HCT (Top 25%) | 0 | 98 | 162 |

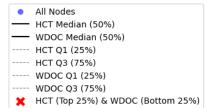


Appendix: Railway Network





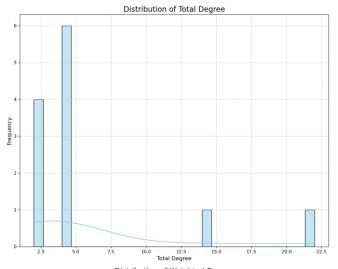


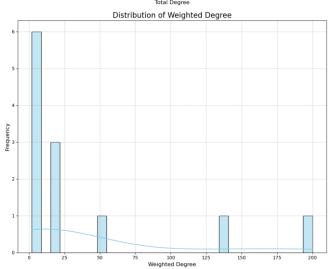


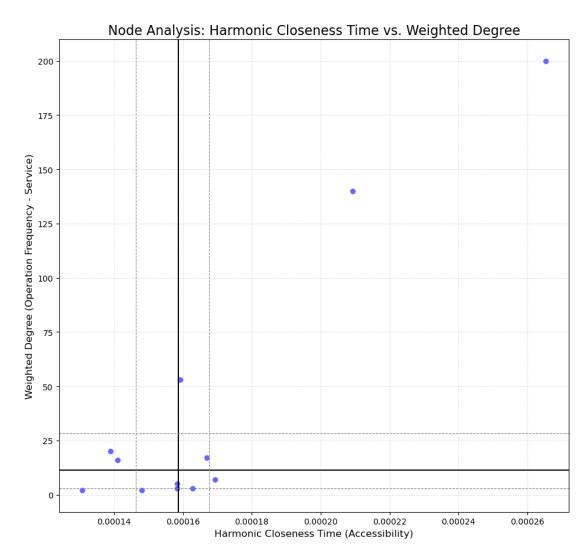
| HCT_Cate gory | WDOC_Category | | |
|--------------------------|---------------------------|-------------------------|---------------------|
| | L_WDOC (Bottom 25%) | M_WDOC (25%- 75%) | H_WDOC (Top 25%) |
| L_HCT (Bottom 25%) | 33 | 23 | 3 |
| M_HCT (25%- 75%) | 27 | 58 | 31 |
| H_HCT (Top 25%) | 9 | 25 | 25 |

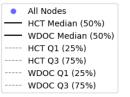


Appendix: Avation Network





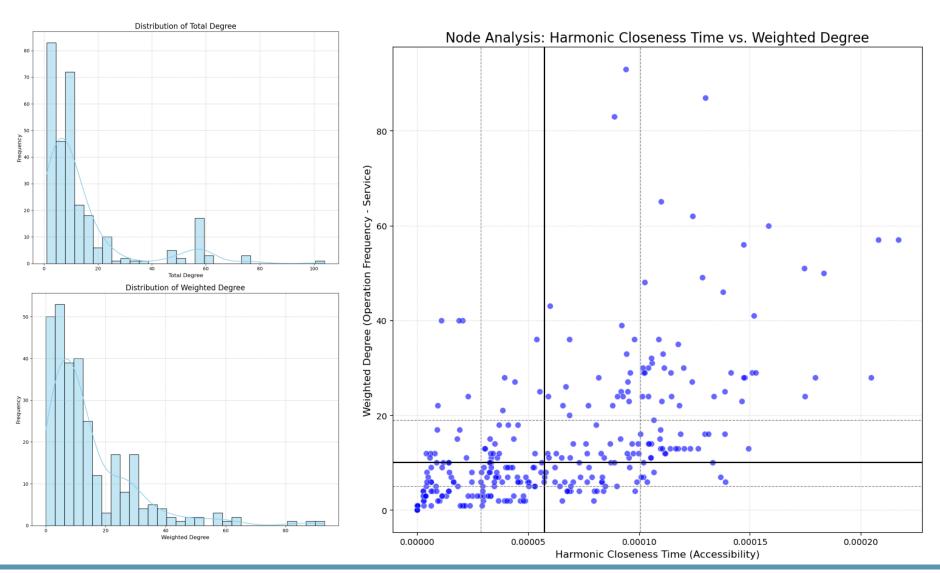




| HCT_Cate gory | WDOC_Category | | |
|--------------------------|---------------------------|-------------------------|---------------------|
| | L_WDOC (Bottom 25%) | M_WDOC (25%- 75%) | H_WDOC (Top 25%) |
| L_HCT (Bottom 25%) | 1 | 2 | 0 |
| M_HCT (25%- 75%) | 3 | 2 | 1 |
| H_HCT (Top 25%) | 0 | 1 | 2 |



Appendix: Maritime Network



| • | All Nodes |
|---|-------------------|
| — | HCT Median (50%) |
| — | WDOC Median (50%) |
| | HCT Q1 (25%) |
| | HCT Q3 (75%) |
| | WDOC Q1 (25%) |
| | WDOC Q3 (75%) |
| | |

| HCT_Cate gory | WDOC_Category | | |
|--------------------------|---------------------------|-------------------------|---------------------|
| | L_WDOC (Bottom 25%) | M_WDOC (25%- 75%) | H_WDOC (Top 25%) |
| L_HCT (Bottom 25%) | 43 | 26 | 5 |
| M_HCT (25%- 75%) | 36 | 84 | 26 |
| H_HCT (Top 25%) | 0 | 31 | 42 |



Appendix: HCT & WDOC Multimodal Network

